

1. The following is a partially completed Cayley table for a group.

	1	2	3	4	5	6	7	8
1	1	2	3	4	5	6	7	8
2	2	1	4	3	6	5	8	7
3	3	4	2	1	7	8	6	5
4	4	3	1	2	8	7	5	6
5	5	6	8	7	1			
6	6	5	7	8		1		
7	7	8	5	6			1	
8	8	7	6	5				1

- (a) Complete the Cayley table.
- (b) Find the centralizer of each member of the group.
- (c) Find $Z(G)$.
- (d) What is the order of 2? 3? 4?
- (e) Find a proper subgroup, H , containing 2 and 3.
- (f) Is H cyclic? If so, what is a generator?

2. Let H_1, H_2, H_3, \dots be a sequence of subgroups of a group with the property that $H_1 \subseteq H_2 \subseteq H_3 \dots$. Prove that the union of the sequence is a subgroup.