

## Momentum and Energy

Chapter 3

## Momentum



- Momentum is inertia in motion
- **Mass x velocity**
- Has both magnitude and direction
- Large mass or high speed can give object great amount of momentum

## Momentum = $m \cdot v$

- Change momentum by
  - changing mass
  - or velocity—usually velocity
- What causes changes in velocity?
- Force
- Time is also important

## Momentum and Impulse

- Apply force over time to change velocity and momentum
- Greater time of application, greater change in momentum
- Force x time interval is IMPULSE



## Impulse = $F \cdot t$

- Force x time interval
- Impulse changes momentum
- Technically:  $Ft = \Delta(mv)$
- Realistically:  $Ft = m\Delta v$

## Impulse Increasing Momentum

$$Ft = m\Delta v$$

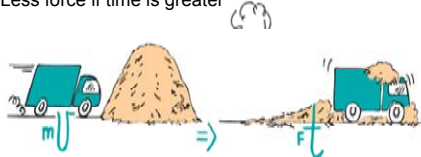
- Pushing a child on a swing—the force
- Increases momentum
- Longer push increases momentum more than a short one



<http://www.bcm.edu/oto/research/cochisea/Volta/16.html>

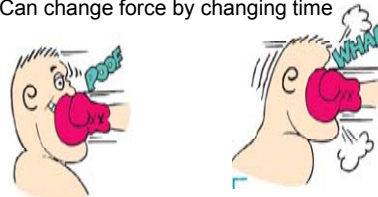
## Impulse Decreasing Momentum

- Stopping the out of control car  $Ft = m\Delta v$
- Change momentum to zero
- Less force if time is greater



## Impulse Changes Momentum

- Can change force by changing time



- Move away increases time, reduces force
- Toward decreases time, increases force

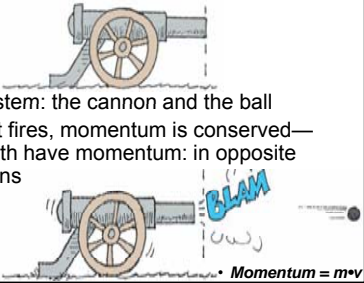
## Bounce increases impulse

$$Ft = m\Delta v$$

- There is a change in velocity direction, making a greater  $\Delta v$
- So greater force is required
- Water changes direction, has greater impulse than a flat paddle



### Conservation of Momentum



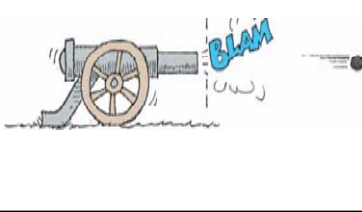
- The system: the cannon and the ball
- When it fires, momentum is conserved—they both have momentum: in opposite directions

•  $Momentum = m \cdot v$

### Conservation of Momentum

- No net force
- No net momentum

•  $Momentum = m \cdot v$

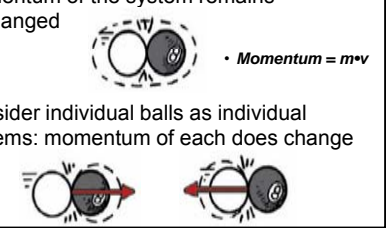


### Conservation of Momentum

- In the absence of external force, the momentum of the system remains unchanged

•  $Momentum = m \cdot v$

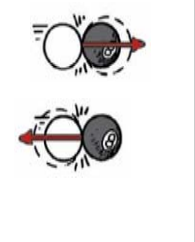
- Consider individual balls as individual systems: momentum of each does change



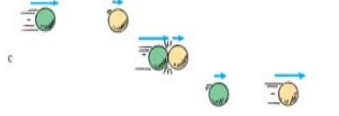
### Conservation of Momentum

- Net momentum is the same before the collision
- As after the collision

•  $Momentum = m \cdot v$



### Conservation of Momentum



- Yellow ball starts stationary
- Both balls moving opposite directions
- Green ball moving faster

•  $Momentum = m \cdot v$

### Energy

- Property of a system that enables it to do work
- Potential Energy
  - Springs
  - Chemicals
  - Gravity
- Kinetic Energy

### Potential Energy




• <http://www.howstuffworks.com/inside-clock.htm>

• [http://www.illigen.com/Redneck/redneck\\_1samnmower.htm](http://www.illigen.com/Redneck/redneck_1samnmower.htm)

### Potential Energy

- Fuel is chemical potential energy




• <http://www.alternativefuels.com.au/Biodiesel/dragster.htm>

• [http://www.illigen.com/Redneck/redneck\\_1samnmower.htm](http://www.illigen.com/Redneck/redneck_1samnmower.htm)

### Work is Energy

- Lift heavy ram of pile driver
- Work transfers energy to lift into gravitational potential energy



### Gravitational potential energy

- Due to object's position
- Relative to a surface
- = weight x height =  $mgh$
- Work done for object to gain potential energy

### Gravitational potential energy



### Gravitational potential energy

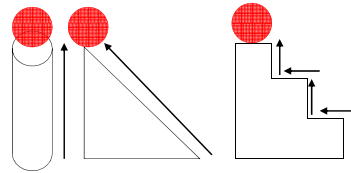
- $E_p = \text{mass} \times (\text{acceleration of gravity}) \times \text{height}$
- Height is above some reference level  
Potential energy is always referenced to a zero level defined in the system

### Gravitational potential energy

- $E_p = mgh$
- $mg = \text{weight}$
- $h = \text{height}$

### Gravitational potential energy

- $E_p = mgh$
- Path to the height is not factor in  $E_p$
- Horizontal distance is not factor in  $E_p$



### Kinetic Energy of Motion

- $E_k = \frac{1}{2}mv^2$
- Work is a change in kinetic energy
- $W = \Delta E_k$
- $\Delta$  Delta 'change'

### Kinetic Energy of Motion

- Heat
- Sound
- Electricity and light

### Kinetic Energy of Motion

- $W = \Delta E_k$  Work is change in kinetic energy
- Work-energy theorem
- Net work = force x distance  $W = Fd$ 
  - Due to net force

$$E_k = \frac{mv^2}{2}$$

$$Fd = \frac{mv^2}{2}$$

### Conservation of Energy

- Cannot be created or destroyed
- Can be converted from one form to another

### Kinetic energy and momentum

- Properties of moving things
- Momentum is a vector quantity
  - can be cancelled with opposite momentum
- Kinetic Energy is a scalar quantity
  - Cannot ever be cancelled



[http://www.littletheatre.net/Firecracker\\_Misamis\\_firecracker\\_contest.htm](http://www.littletheatre.net/Firecracker_Misamis_firecracker_contest.htm)

### Conservation of Energy

- Transformation from one form to another
- Potential energy of stretched rubber of slingshot
- Transformed to kinetic energy of rock flying through air



### Conservation of Energy

- Rock transfers its kinetic energy to the object it hits
- May be transformed to heat upon impact
- Energy cannot be created or destroyed



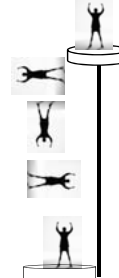
### Conservation of Energy



<http://science.howstuffworks.com/roller-coaster.htm>

### Conservation of Energy

- $E_p = 10000 \text{ J}$   $E_k = 0 \text{ J}$
- $E_p = 7500 \text{ J}$   $E_k = 2500 \text{ J}$
- $E_p = 5000 \text{ J}$   $E_k = 5000 \text{ J}$
- $E_p = 2500 \text{ J}$   $E_k = 7500 \text{ J}$
- $E_p = 0 \text{ J}$   $E_k = 10000 \text{ J}$



### Conservation of Energy

- Does a car use more energy when its lights are on?
- What about when the air conditioner is on?
- How about using the radio when the engine is off?

### Work

Transference of Energy  
 Work = Force x distance

$$W = Fd$$

Work into system = work out of system

### Work

- Lifting load against the force of the weight of the object
- Move an object twice as far results in twice the work
- Move two object (Twice the weight) the same distance as one is twice the work
- Nothing about time in definition
- Slow or fast
- Same force, same distance = same work

### Work $W = Fd$

- Twice the weight
- Twice the distance



### Work $W=Fd$

- Units of work are Newton-meters, same as Joules

$$\mathbf{F} \cdot \mathbf{d} = \mathbf{N} \cdot \mathbf{m} = \frac{\mathbf{kg} \cdot \mathbf{m}}{\mathbf{s}^2} \cdot \mathbf{m} = \frac{\mathbf{kg} \cdot \mathbf{m}^2}{\mathbf{s}^2} = \mathbf{J}$$

- SO Work is energy

### Work is Energy

- Same units
- Work occurs with transfer of energy
- Work occurs when you store potential energy

### Work is Energy

Mechanical energy

Moving things—has two forms

1. Potential mechanical energy  
Waiting to work
2. Kinetic mechanical energy  
Work being done

### Work is Energy

- Energy stored in bow
- Work is done to create the potential energy



### Power

- Work done over time

$$\text{Power} = \frac{\text{Work done}}{\text{time interval}}$$

- Units:  $\frac{\text{kg} \cdot \text{m}^2}{\text{s}^3} = \text{watt}$

### Power

$$P = \frac{\text{energy}}{\text{time}}$$

- Half the time  
=Twice the power
- Twice the time  
=Half the power

### Power: $P = \text{energy}/\text{time}$

- Fuel burn
- Biodiesel



<http://www.alternativefuels.com.au/Biodiesel/dagster.htm>

[http://www.lilligen.com/Redneck/redneck\\_lawnmower.htm](http://www.lilligen.com/Redneck/redneck_lawnmower.htm)

### Work, Energy and Power



Water behind the dam

Potential energy

Convert it to electrical energy

### Work and Energy

- $E_P$  transformed to another form of energy
- Kinetic energy of motion