

Momentum and Energy

Chapter 3

Momentum



- Momentum is inertia in motion
- **Mass x velocity**
- Has both magnitude and direction
- Large mass or high speed can give object great amount of momentum

$$\mathbf{Momentum = m \cdot v}$$

- Change momentum by
 - changing mass
 - or velocity—usually velocity
- What causes changes in velocity?
- Force
- Time is also important

Momentum and Impulse

- Apply force over time to change velocity and momentum
- Greater time of application, greater change in momentum
- Force x time interval is **IMPULSE**



Impulse = $F \cdot t$

- Force x time interval
- Impulse changes momentum
- Technically: $Ft = \Delta(mv)$
- Realistically: $Ft = m\Delta v$

Impulse Increasing Momentum

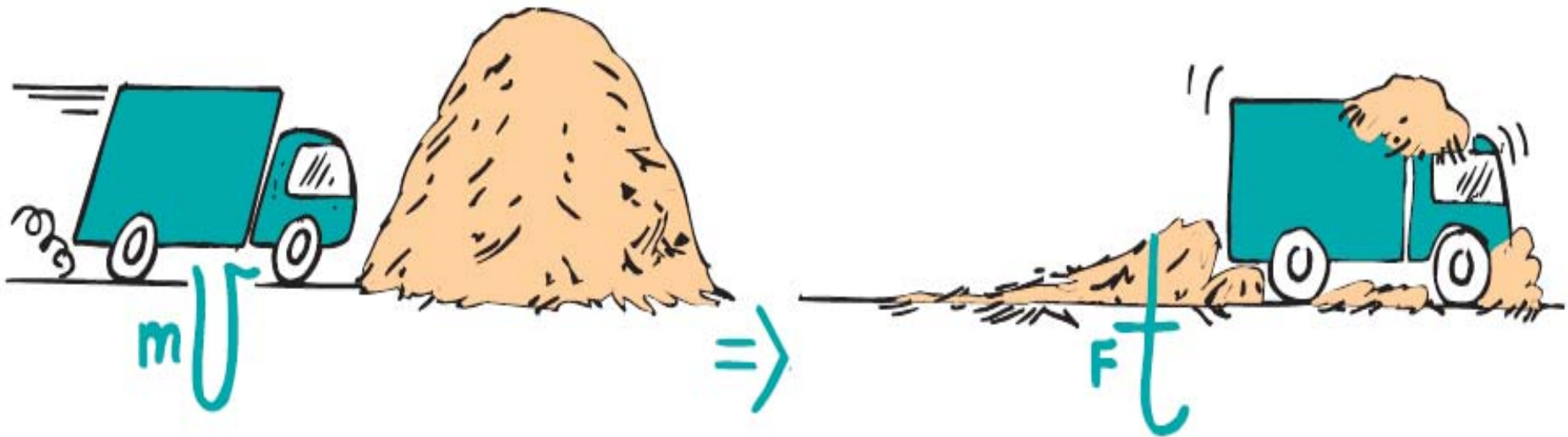
$$Ft = m\Delta v$$

- Pushing a child on a swing—the force
- Increases momentum
- Longer push increases momentum more than a short one



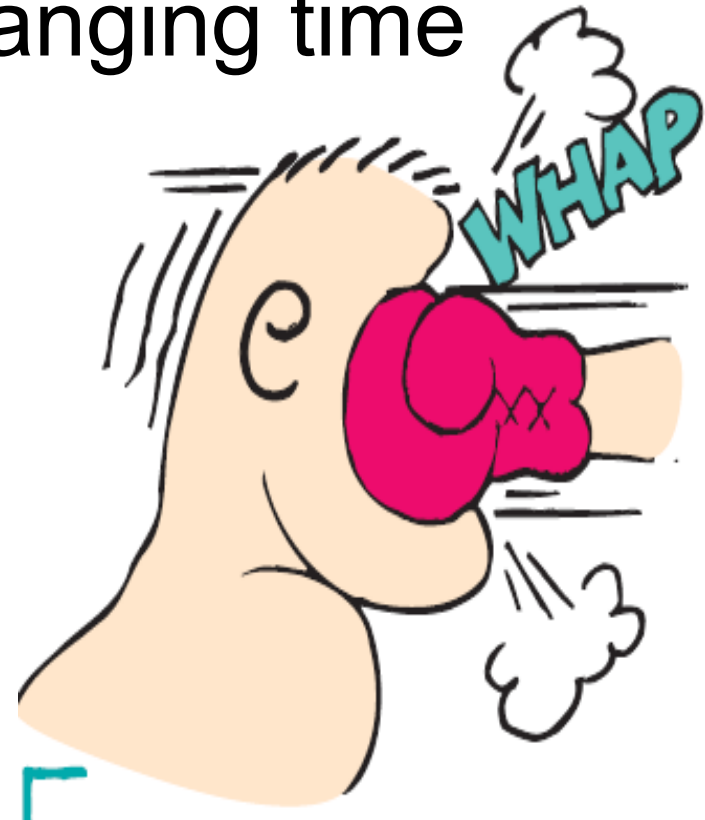
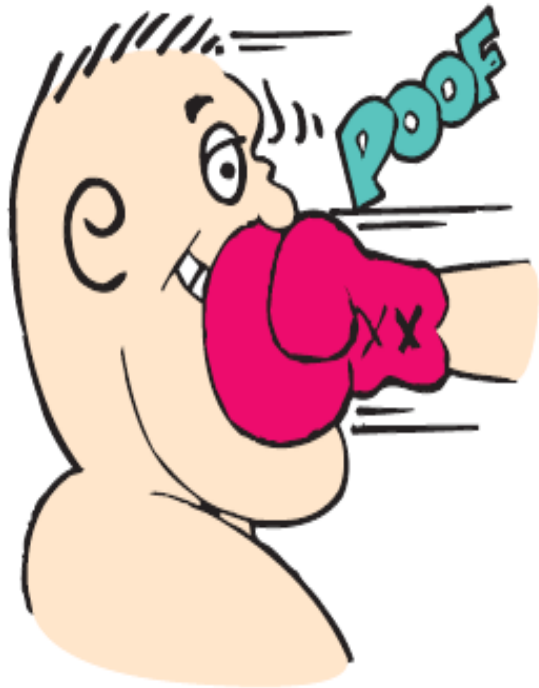
Impulse Decreasing Momentum

- Stopping the out of control car $Ft = m\Delta v$
- Change momentum to zero
- Less force if time is greater



Impulse Changes Momentum

- Can change force by changing time

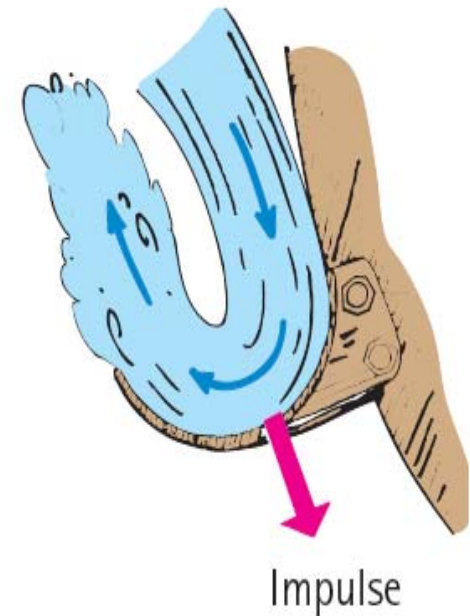


- Move away increases time, reduces force
- Toward decreases time, increases force

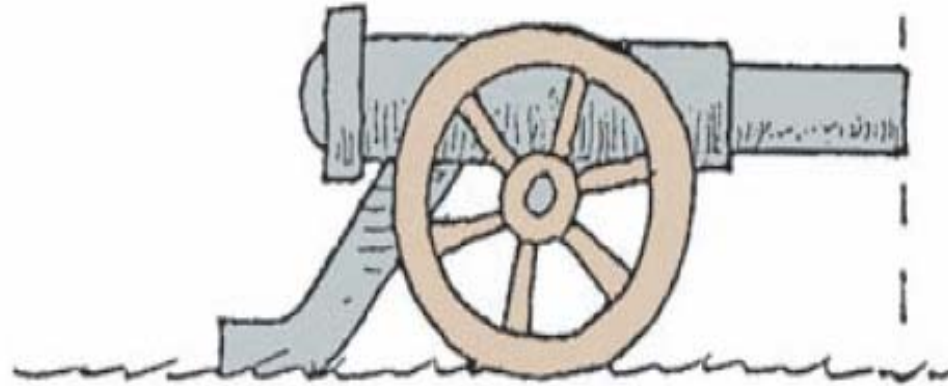
Bounce increases impulse

- There is a change in velocity direction, making a greater Δv
- So greater force is required
- Water changes direction, has greater impulse than a flat paddle

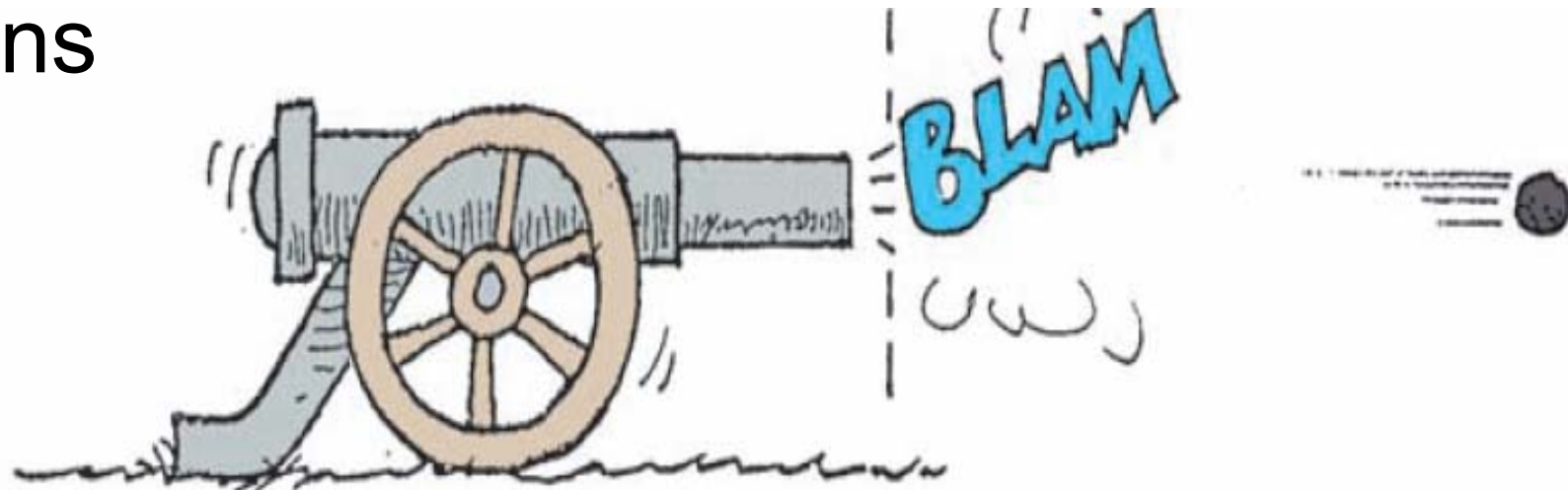
$$Ft = m\Delta v$$



Conservation of Momentum

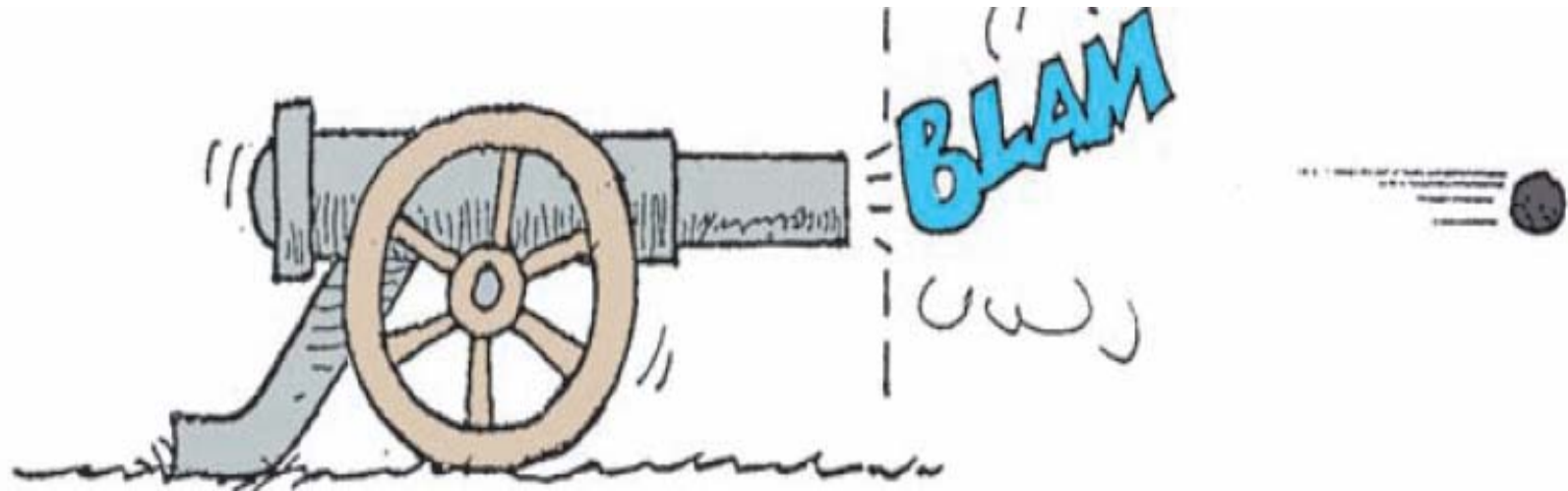


- The system: the cannon and the ball
- When it fires, momentum is conserved— they both have momentum: in opposite directions



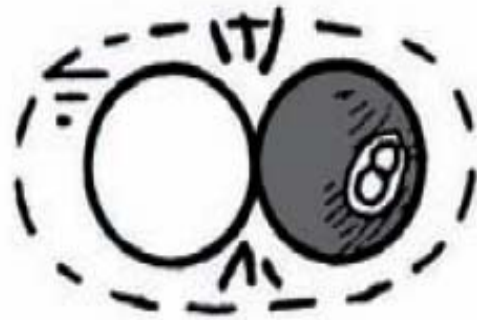
Conservation of Momentum

- No net force
- No net momentum

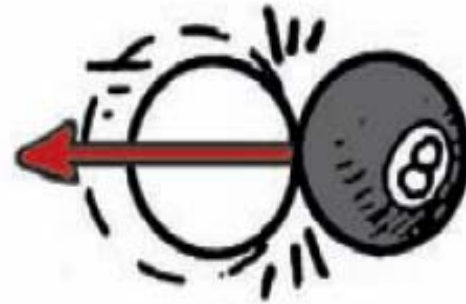


Conservation of Momentum

- In the absence of external force, the momentum of the system remains unchanged

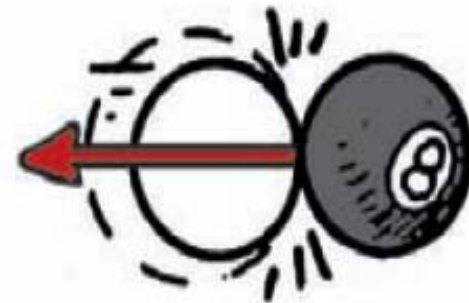


- Consider individual balls as individual systems: momentum of each does change

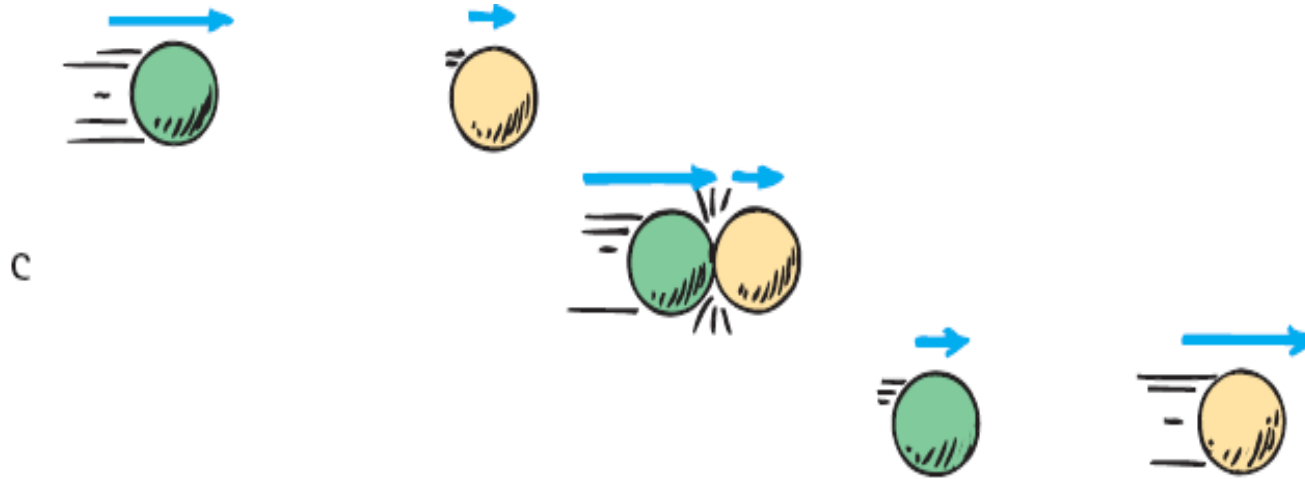


Conservation of Momentum

- Net momentum is the same before the collision
- As after the collision



Conservation of Momentum



- a. Yellow ball starts stationary
- b. Both balls moving opposite directions
- c. Green ball moving faster

Work

Transference of Energy

Work = Force x distance

$$W = Fd$$

***Work* $W=Fd$**

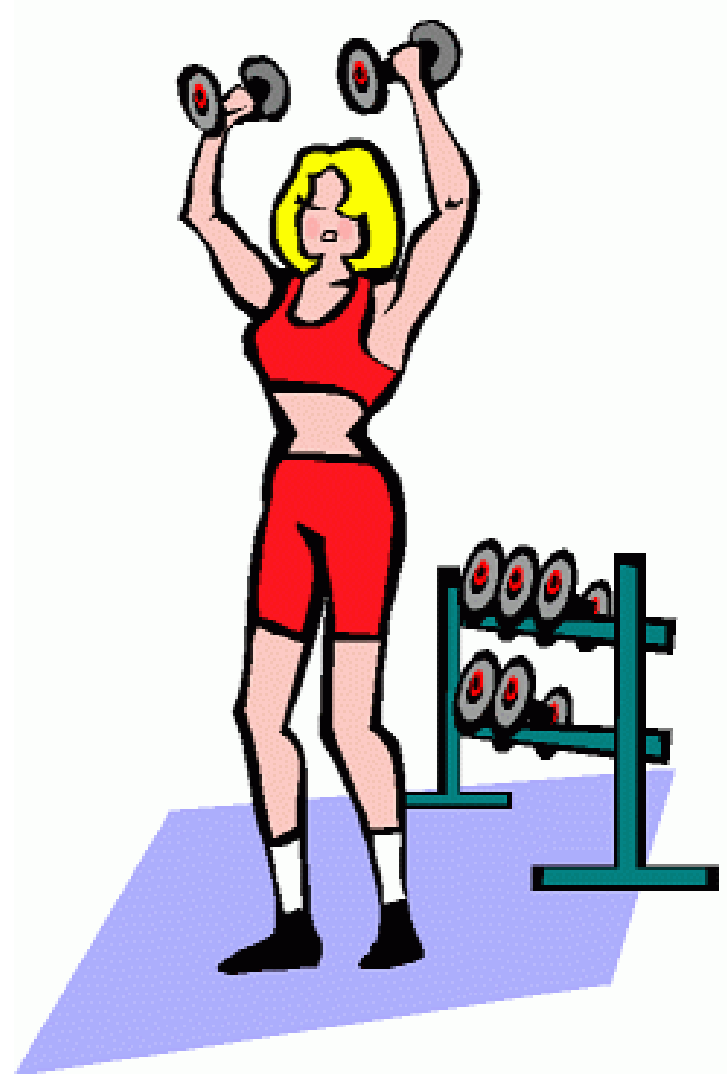
- Nothing about time in definition
- Slow or fast
- Same force, same distance = same work

Work

- Lifting load against the force of the weight of the object
- Twice the distance results in twice the work
- Twice the weight is twice the work

Work $W=Fd$

- Twice the weight
- Twice the distance



***Work* $W=Fd$**

- Units of work are Joules
- Work is energy

Work $W=Fd$

Units of force : Newtons = $\frac{kg \cdot m}{s^2}$

Force x distance : Newton meters

$$= \frac{kg \cdot m}{s^2} \cdot m = \frac{kg \cdot m^2}{s^2}$$

=Joules

Work $W=Fd$

- Weight lifter does work to lift barbell
- expends energy to keep the potential energy in the barbell
- But he does no work on the barbell after it is lifted



Work vs. Energy

- Same units
- Work occurs with transfer of energy
- Work occurs when you store potential energy

Work vs. Energy

Mechanical energy

Moving things—has two forms

1. Potential mechanical energy

Waiting to work

2. Kinetic mechanical energy

Work being done

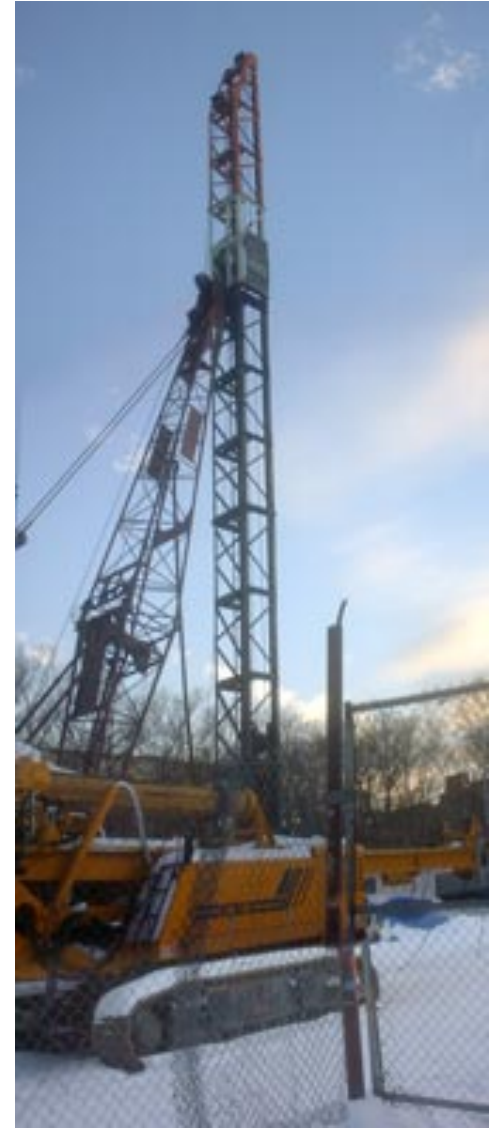
Work vs. Energy

- Energy stored in bow
- Work is done to create the potential energy

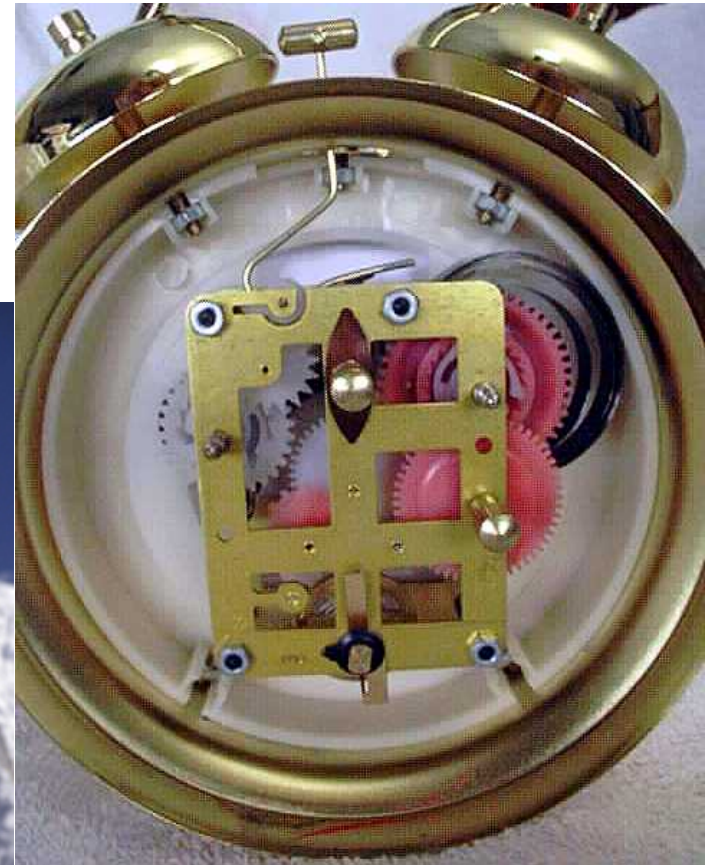


Work vs. Energy

- Lift heavy ram of pile driver
- Work transfers energy to lift into potential gravitational energy



Potential Energy



<http://www.howstuffworks.com/inside-clock.htm>

- http://www.himalayan.pdx.edu/virtualjourney/slideshow/se_photos_web/pages/Boy%20with%20Slingshot%2C%20J.htm

Potential Energy

- Fuel is chemical potential energy



http://www.lilligren.com/Redneck/redneck_lawnmower.htm



<http://www.alternativefuels.com.au/Biodiesel/dragster.htm>

Gravitational potential energy

- Due to object's position
- Relative to a surface

Gravitational potential energy

= weight x height = mgh

- Work done for object to gain potential energy

Gravitational potential energy



Gravitational potential energy

$E_p = \text{mass} \times \text{acceleration of gravity} \times \text{height}$

Height is above some reference level

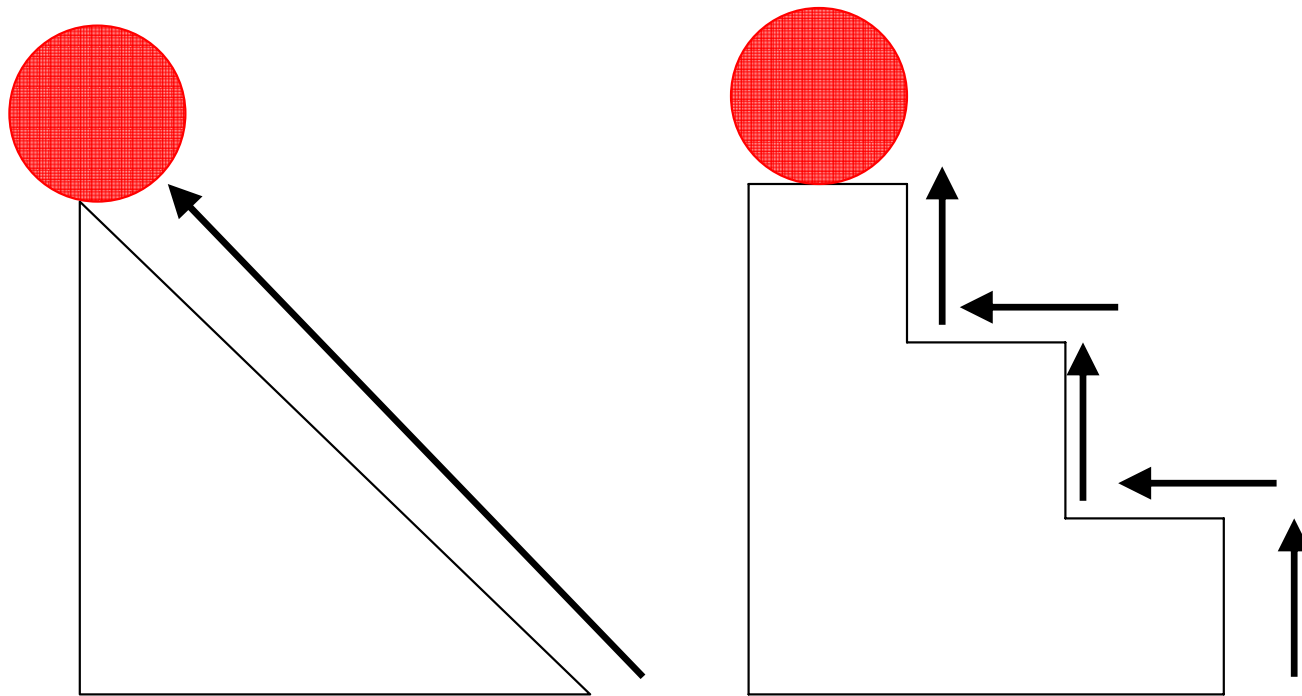
Potential energy is always referenced to a zero level defined in the system

Gravitational potential energy

- $E_p = mgh$
- $mg = \text{weight}$
- $h = \text{height}$

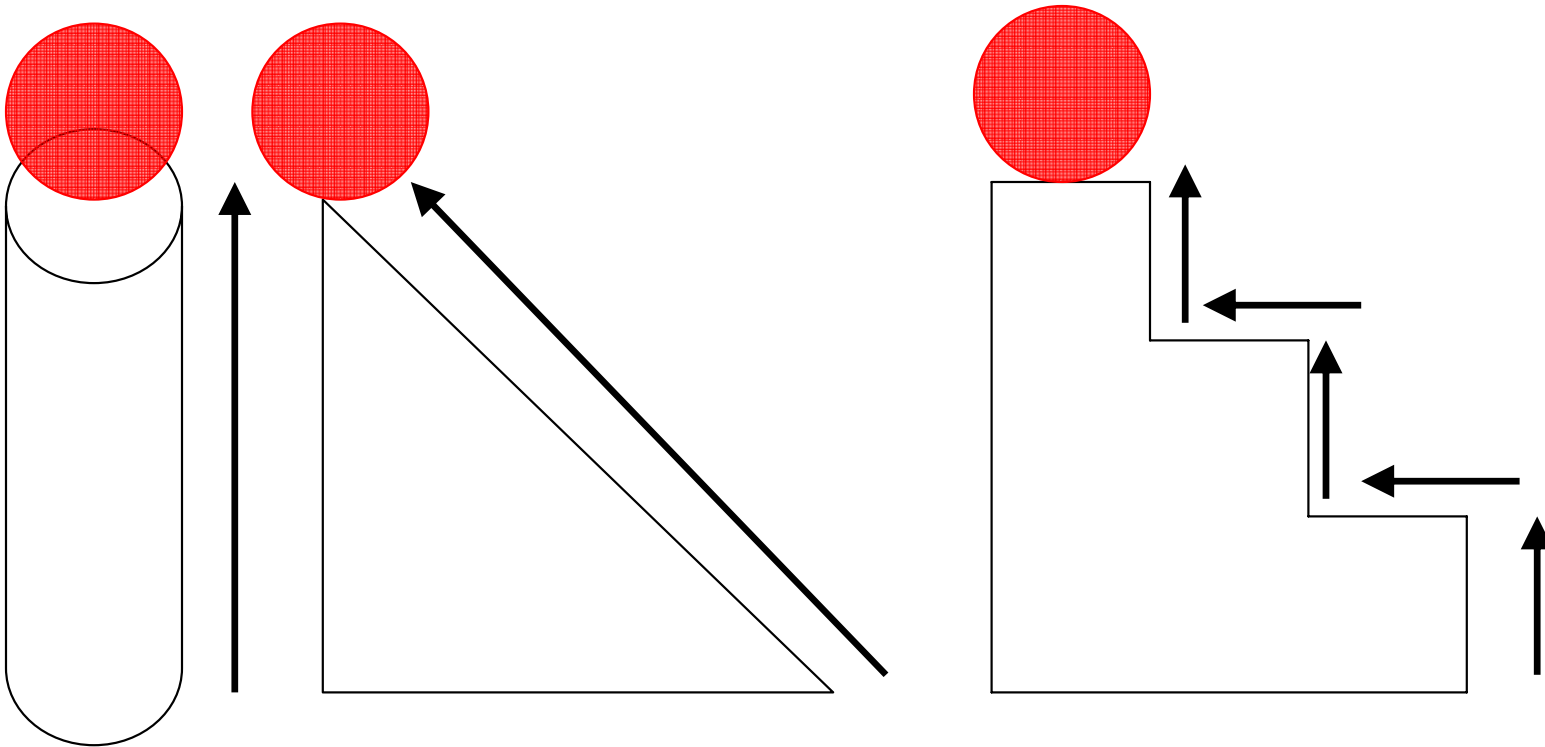
Gravitational potential energy

- $E_p = mgh$
- Path to the height is not factor in E_p



Gravitational potential energy

- $E_p = mgh$
- Horizontal distance is not factor in E_p



Kinetic Energy of Motion

- $E_K = \frac{1}{2} mv^2$
- Work is a change in kinetic energy
- $W = \Delta E_K$
- Δ Delta 'change'

Kinetic Energy of Motion

- How much further will a car skid if you lock up the wheels at 90 km/h vs. 30 km/h?
- $E_K = \frac{1}{2} mv^2$
- $\frac{1}{2} \text{ mass} \times (90 \text{ km/h})^2 = \frac{1}{2} \text{ mass} \times 8100 \text{ km}^2/\text{h}^2$
- $\frac{1}{2} \text{ mass} \times (30 \text{ km/h})^2 = \frac{1}{2} \text{ mass} \times 900 \text{ km}^2/\text{h}^2$
- $\frac{1}{2} \text{ mass} \times 8100 / \frac{1}{2} \text{ mass} \times 900 = 9$
- Nine times further!

Kinetic Energy of Motion

- Heat
- Sound
- Electricity and light

Work-Energy Theorem

- Work is change in kinetic energy

$$*Work = \Delta KE*$$

Kinetic Energy of Motion

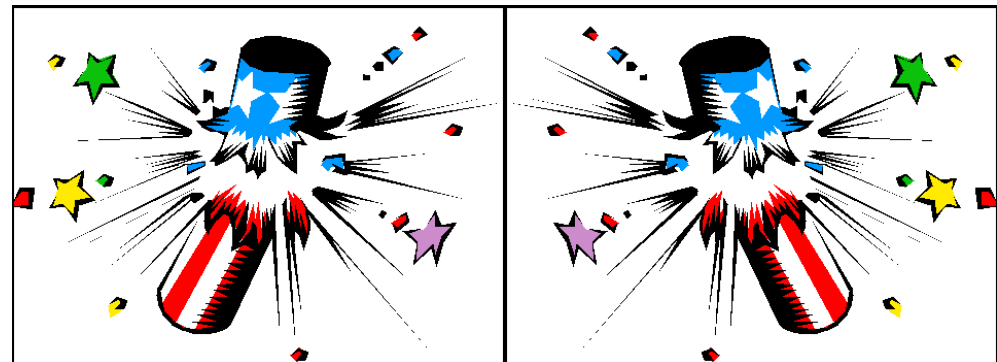
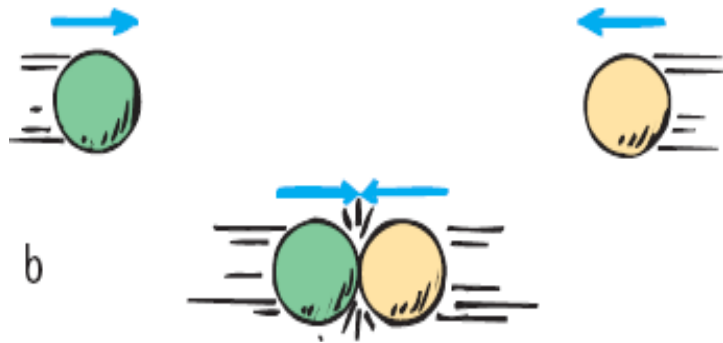
- $W = \Delta E_K$
- Work-energy theorem
- Net work = force x distance = Fd
 - Due to net force

$$\bullet E_K = \frac{mv^2}{2}$$

$$\bullet Fd = \frac{mv^2}{2}$$

Kinetic energy and momentum

- Properties of moving things
- Momentum is a vector quantity
 - can be cancelled with opposite momentum
- Kinetic Energy is a scalar quantity
 - Cannot ever be cancelled



Conservation of Energy

- Cannot be created or destroyed
- Can be converted from one form to another

Conservation of Energy

- Transformation from one form to another
- Potential energy of stretched rubber of slingshot
- Transformed to kinetic energy of rock flying through air
- Kinetic energy of rock flying through air = Potential energy of stretched rubber of slingshot
- Transformed from potential to kinetic
- Rock transfers its kinetic energy to the object it hits
- May be transformed to heat upon impact
- Energy cannot be created or destroyed
- It may be transformed from one form into another, but the total amount never changes.



Conservation of Energy

- Sun's energy from fusion of hydrogen to helium



- Sun's energy converted to chemical energy by plants
- Sun's heat converted to potential energy when it evaporates water

Conservation of Energy

- Does a car use more fuel when its lights are on?
- What about when the air conditioner is on?
- How about using the radio when the engine is off?

Power

- Work done over time

$$\text{Power} = \frac{\text{Work done}}{\text{time interval}}$$