Momentum and energy

- I. Momentum
 - A. = Mass x velocity
 - B. Objects of different mass can have same momentuma. Small one going fast = large one going slow

C. Units
$$(kg) \cdot \left(\frac{m}{s}\right)$$

- II. Impulse
 - A. = Force x time
 - B. Change in momentum created by impulse
 - 1. Ft = Δmv , and since v is easier to change, usually Ft = $m\Delta v$

2. Units N·s, or
$$(kg) \cdot \left(\frac{m}{s}\right)$$

- C. Force of the change in momentum can be changed by changing time interval of application of force. See ICA for today's class. Click here for link
- D. Reversing velocity (which is a vector with direction and speed) has greater impulse, resulting in greater force.
- III. Conservation of momentum
 - A. Considering all parts of a system defined as an action-reaction pair, the net momentum is zero
 - B. So in action-reaction pairs, $m_1v_1 + m_2v_2 = 0$
 - C. Cue ball and 8 ball, marble demonstration, cannon-cannonball problem in class (link here)
- IV. Work
 - A. = Force x distance
 - B. Work is force acting over a distance

C. Units: N m, or Joules =
$$(kg) \cdot \left(\frac{m}{s^2}\right) \cdot m = \frac{kg \cdot m^2}{s^2}$$

- D. Change in force or change in distance increases work done
- E. Directly proportional to the change

- V. Energy
 - A. Property of a system that allows it to do work
 - B. Application of force and movement caused by that force
 - C. Mechanical energy: two types
 - a. Potential energy: waiting to work
 - 1) Springs, weights above a reference level
 - 2) Gravitational potential energy = weight x height
 - i. $E_P = mgh$ —units:

a.
$$E_p = kg \cdot \frac{10m}{s^2} \cdot m = \frac{kg \cdot m^2}{s^2} = J$$

- b. (Joules)
- ii. Gravitational potential energy dependent upon height
- b. Kinetic energy: moving object doing work
 - 1) Depends on mass and speed

$$E_{K} = \frac{1}{2} \mathbf{m} \cdot \mathbf{v}^{2} = \frac{\mathbf{m} \cdot \mathbf{v}^{2}}{2}$$

BE CAREFUL to only square the velocity

- 3) When velocity is squared, the energy loses its direction
- 4) Kinetic energy is not a vector; it has magnitude but cannot be canceled, (unlike momentum that can be canceled)
- VI. Work Energy Theorem
 - A. Work = change in Kinetic energy
 - B. Energy is conserved—
 - 1. Gravitational potential energy is changed into kinetic energy of motion as things fall
 - 2. In system without loss of energy to friction or heat, all of the E_P would change to E_K or back again in pendulum, in roller coaster, in the acrobats Art and Bart from page 75 of textbook.

VII. Power

A. =
$$\frac{\text{work done}}{\text{time interval}}$$

B. Units: = $\frac{\text{Joules}}{\text{second}} = \frac{\left(\frac{\text{kg} \cdot \text{m}^2}{\text{s}^2}\right)}{\text{s}} = \frac{\text{kg} \cdot \text{m}^2}{\text{s}^3} = \text{watts}$

- C. Power does depend on time interval that work is done.
 - 1. less time, more power required
 - 2. more time, less power