

1. Find the derivative of each of the following using the Product or Quotient Rules as appropriate. Show your work. Don't simplify unless you are asked to.

a. $y = (1 + 3x)(1 + 5x)$

b. $y = (1 + 2x + 3x^3)(1 + 4x + 8x^2)$

c. $y = \sin(x) \left(7x^3 - \frac{1}{x} \right)$

d. $y = \frac{8x}{e^x}$

e. $y = (1 + 3x)(x^3 + 5x)(2 + 3x - 2x^7)$ Hint: You will need to apply the Product Rule twice.

f. $y = \frac{1 + 3x}{1 + 5x}$; simplify the numerator of the derivative.

g. $y = \frac{x^3}{1 + 5x}$; simplify the numerator of the derivative.

2. For $n \in \mathbb{R}$, find the derivative of $y = \frac{1}{x^n}$ by 1) using the Quotient Rule (simplify completely) and by 2) using the Power Rule. Which way is easier?

3. Find the derivative of $y = \frac{1 + 5x}{x^3}$ by 1) using the Quotient Rule (simplify completely) and by 2) simplifying the function first into two fractions and then using the Power Rule on each fraction. Which way is easier?